

Hierarchy of Spin and Valley Symmetry Breaking in Quantum Hall Single Layer Graphene

arXiv: 0910.1388

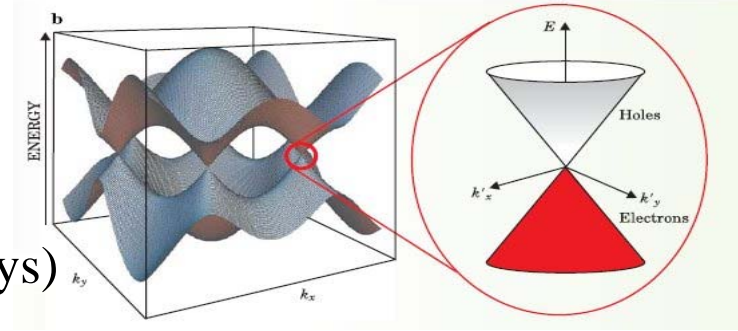
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10/2009 @ Huangshan , China

Graphene and Quantum Hall Effect in Graphene

- Graphene --- a single layer of graphite
 - semiconductor on a honeycomb lattice
 - massless **Dirac**-fermion band structure
 - Two **inequivalent** points **K** and **K'=-K** (valleys)



- In a perpendicular magnetic field B,
 - the spectrum is quantized into **Landau Levels**:

$$E_n = \text{sgn}(n) \sqrt{2e\hbar v_F^2 |n| B}$$

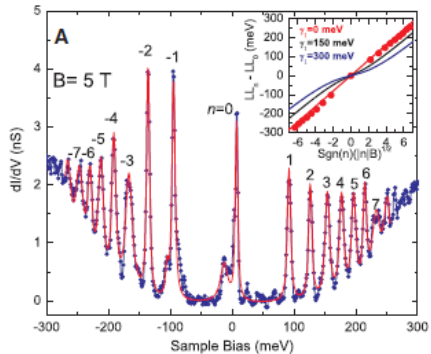
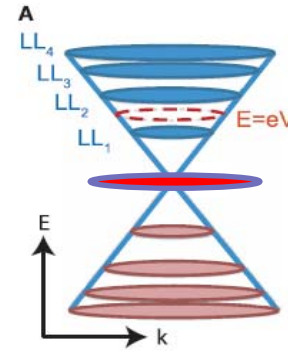
- a quantized **Hall conductance**

$$\sigma_{xy} = \nu \frac{e^2}{h}, \quad \nu = \pm 4 \cdot \left(n + \frac{1}{2}\right)$$

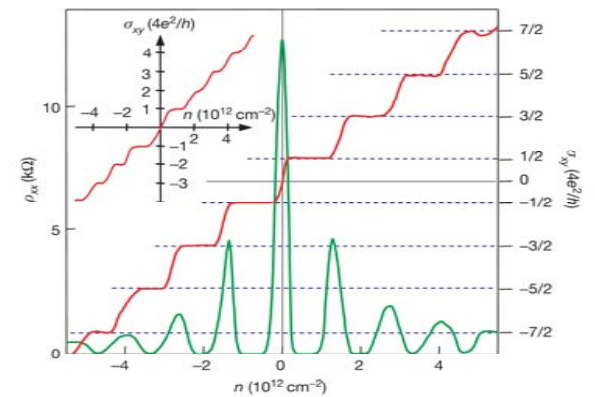
LL degeneracy: spin&valley

- n=integer => $\nu = \dots -6, -2, 2, 6, 10$

- Central Landau Level **n=0**, $E_n=0$, $\nu=-2,+2$



Stroscio group, Science 324, 924 (2009)

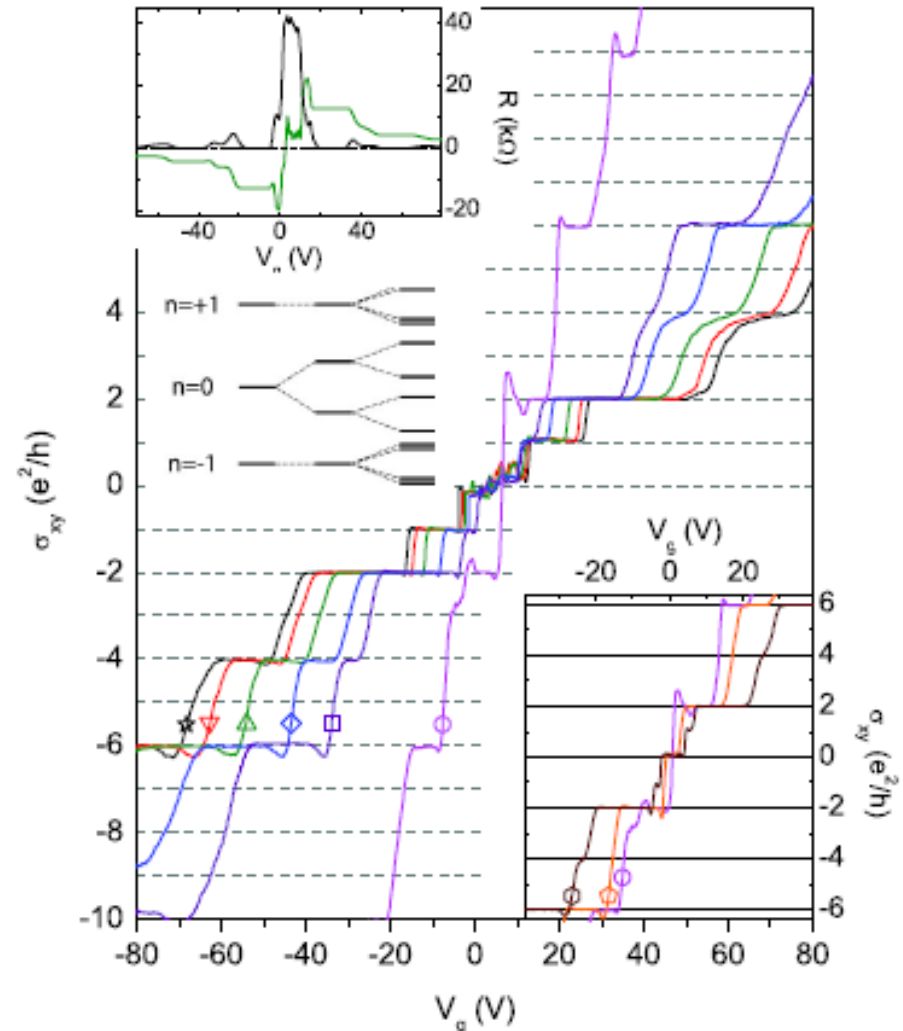


K.S.Novoselov, et.al, Nature 438, 197(2009)

“Only problem” in graphene QHE

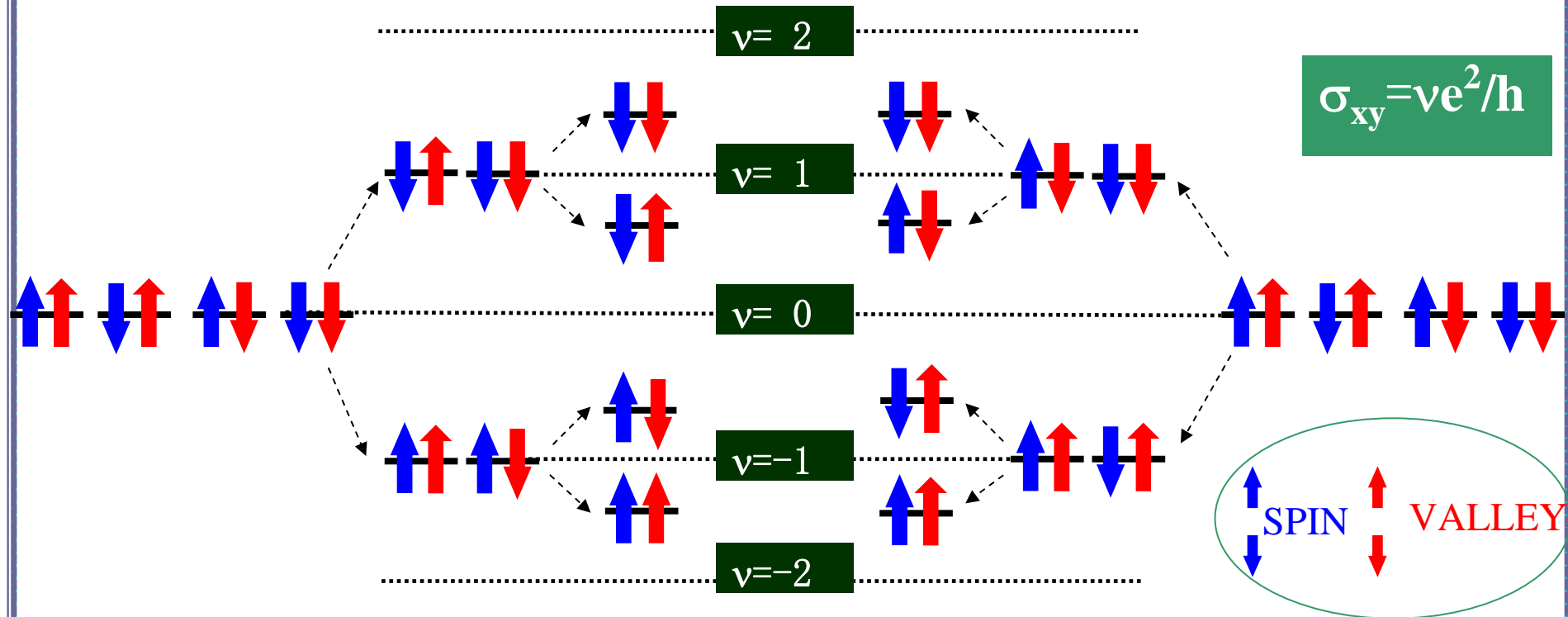
- The spin+valley symmetry of the central LL breaks down at higher magnetic field
- Conductance steps at $-2, +2$
- Conductance steps at $-2, 0, +2$
- Conductance steps at $-2, -1, 0, 1, 2$

B



Y. Zhang, et, al., PRL 96, 136806 (2006)

Which symmetry will be broken first, Spin or valley?



J.G.Checkelsky, L. Li, N.P.Ong, PRL 100, 2008
 PRB 79, 2009
 J. Fuchs, P.Lederer, PRL 98, 2007

D.A. Abanin, P.A.Lee, L.S.Levitov, PRL 96, 2006
 D.A.Abanin, K.S.Novoselov, et.al., PRL 98, 2007
 Z.Jiang, Y.Zhang, et.al, PRL 99, 2007

Mechanisms of symmetry breaking

- LL $n=0 \rightarrow$ Kinetic energy is quenched
- Hamiltonian governing LL physics consists of

σ =spin index
 τ =valley index

- Coulomb exchange (dominant) H^{EX}

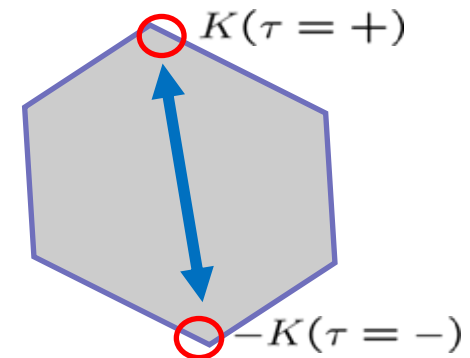
- Zeeman interaction $H^B \sim \sum_{\sigma\tau} \sigma B_{\sigma} \Psi_{\sigma\tau}^{\dagger}(r) \Psi_{\sigma\tau}(r)$

- Valley-scattering impurity $H^{\text{imp}} \sim \sum_{\sigma\tau} \tau V(r) \Psi_{\sigma\tau}^{\dagger}(r) \Psi_{\sigma\tau}(r)$

- Electron-phonon coupling $H^{\text{el-ph}} \sim \sum_{\sigma\tau} \lambda u_{2K} \Psi_{\sigma\tau}^{\dagger}(r) \Psi_{\sigma\bar{\tau}}(r)$

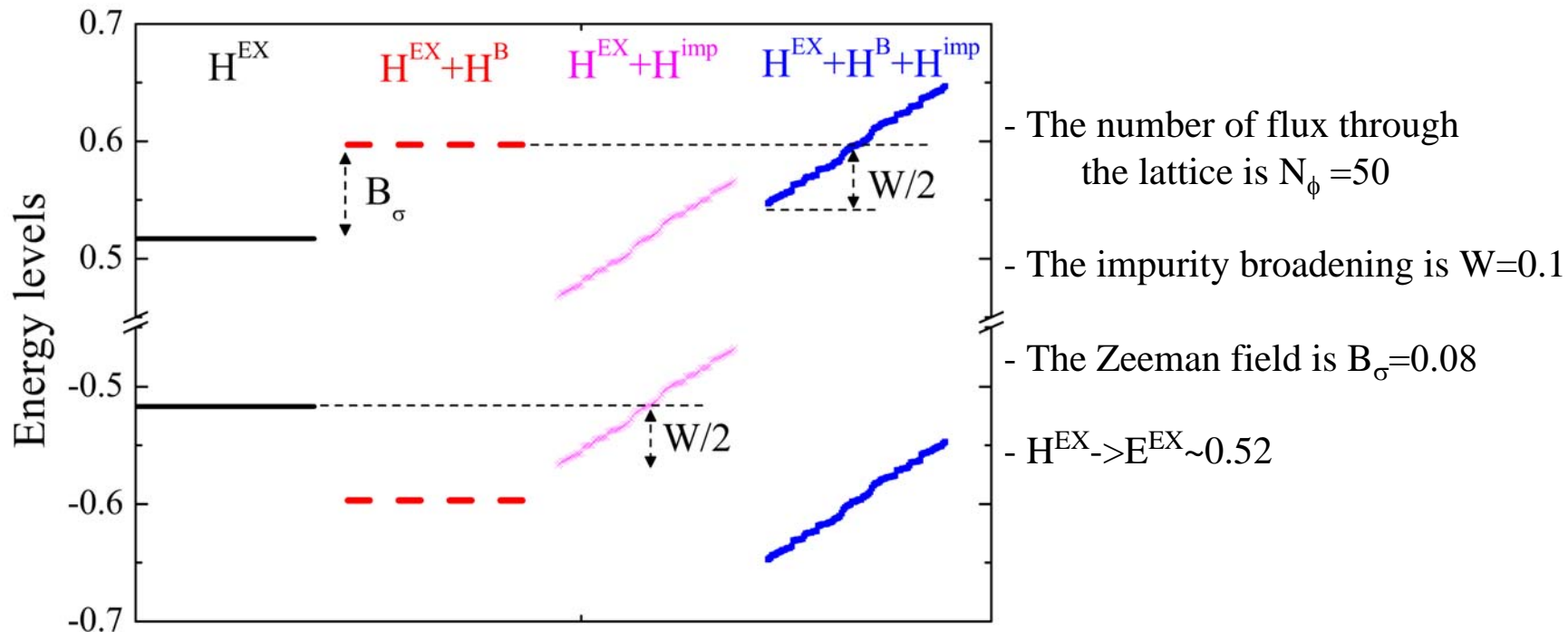
If phonon condenses (Kekule distortion), it will generate effective valley-polarizing field, much like spin-polarizing Zeeman field!

$$\sim \sum_{\sigma\tau} \lambda \langle u_{2K} \rangle \Psi_{\sigma\tau}^{\dagger} \Psi_{\sigma\bar{\tau}} \sim U \sum_{\sigma\tau} \Psi_{\sigma\tau}^{\dagger} \Psi_{\sigma\bar{\tau}}$$



Self-consistent Hartree-Fock theory(SCHFT)

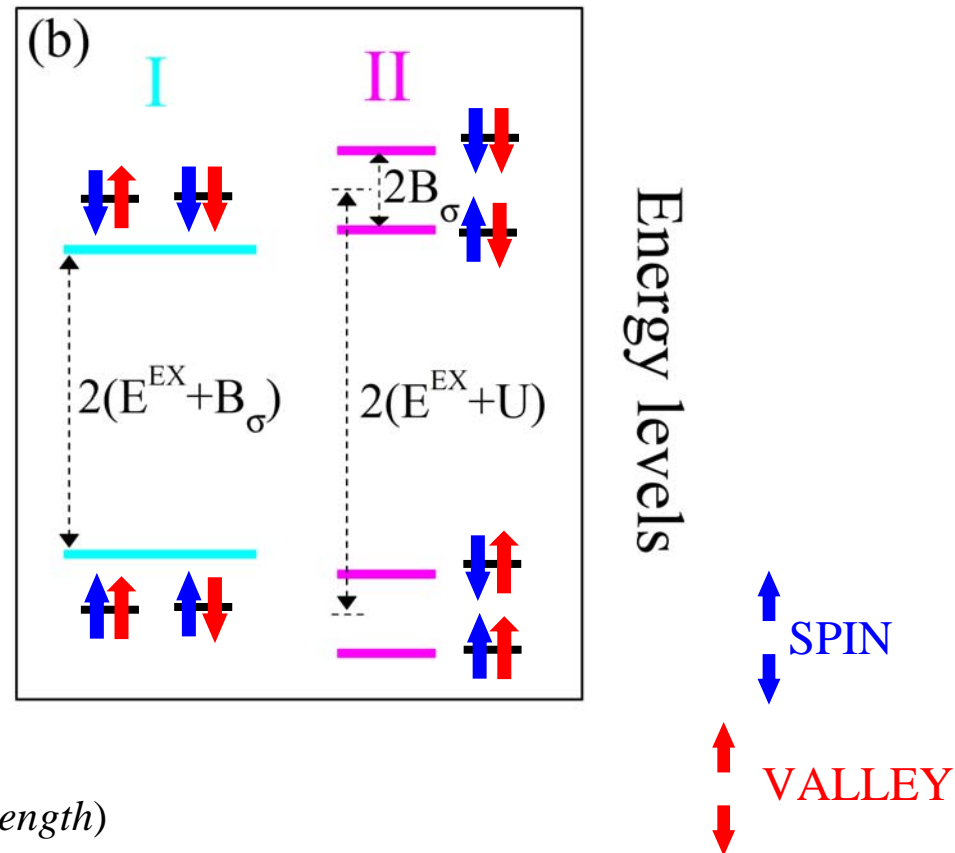
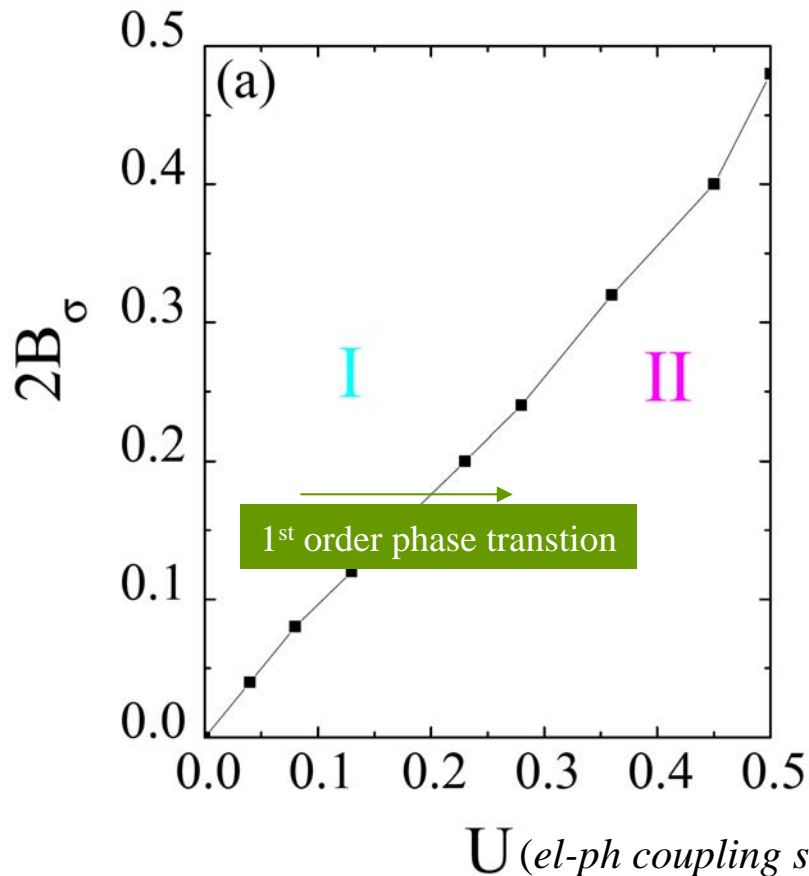
- Energy levels at half-filling from self-consistent solutions



- H^{EX} alone, the initial 4-fold degeneracy of the LL is split into two sublevels : $\pm E^{\text{EX}}$
- Inclusion of Zeeman field to Coulomb exchange \Rightarrow spin-SU(2) symmetry is broken
- Valley-scattering impurity does not result in additional splitting levels and gives rise to broadened energy levels of width W .

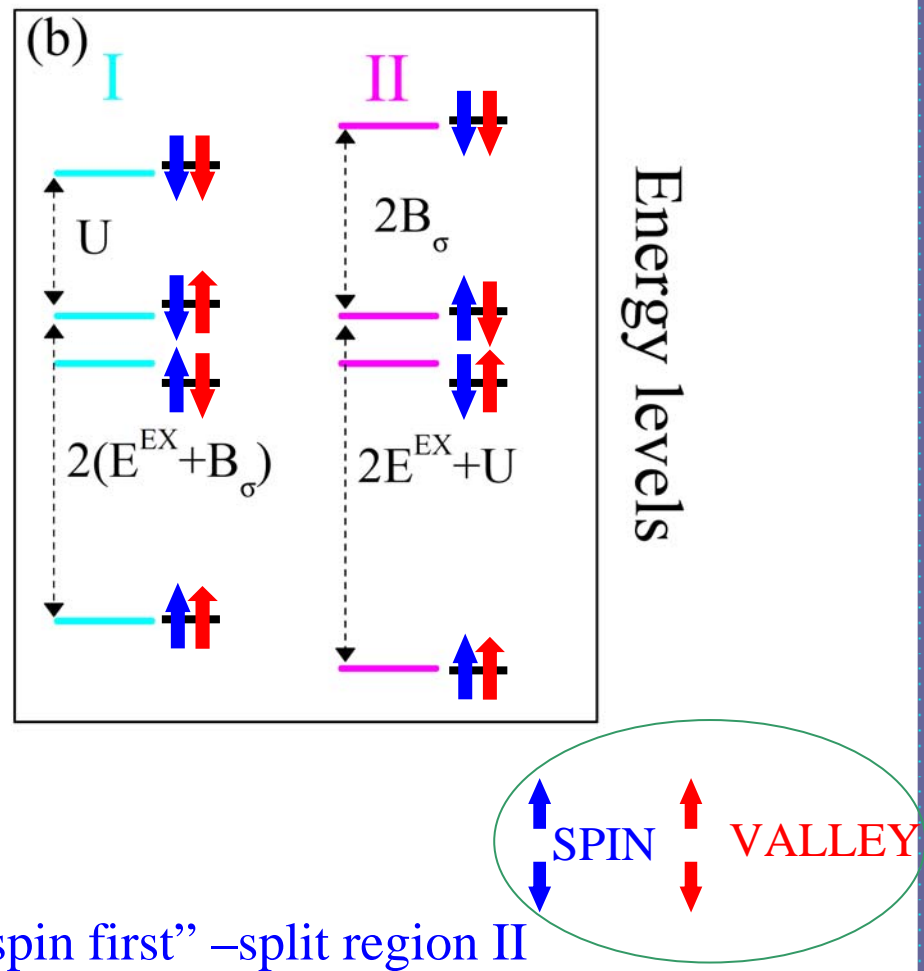
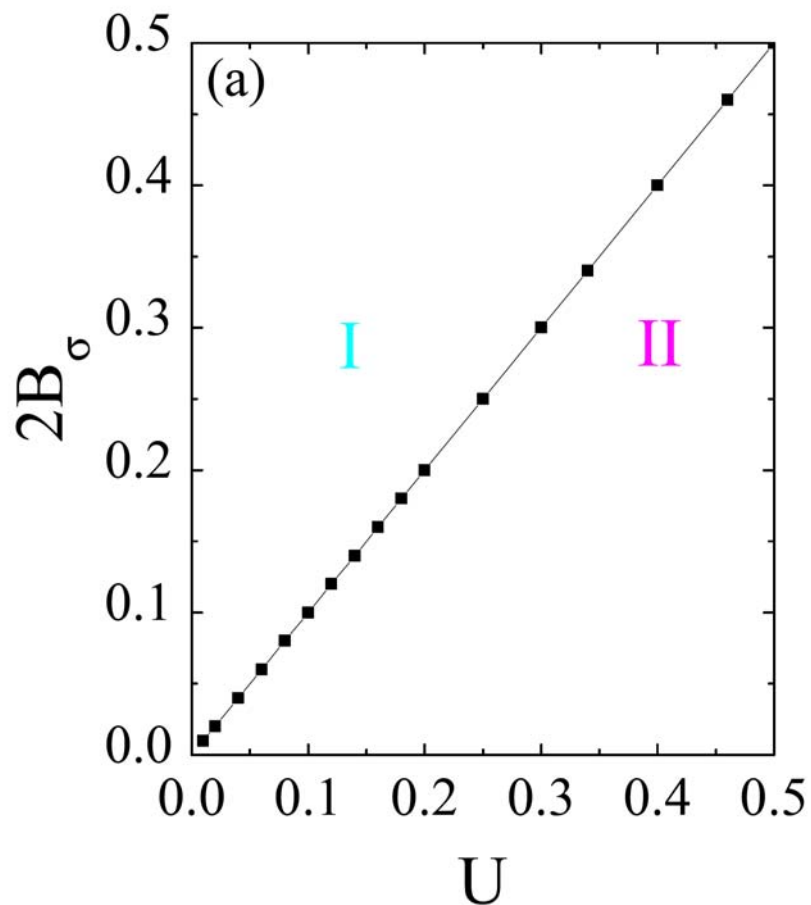
SCHFT: $H^{\text{EX}} + H^{\text{el-ph}} + H^{\text{B}}$ (half-filling case)

(a) Phase diagram of the CLL($n=0$) (b) Schematic energy levels



- In I, Zeeman effect dominates, spin-polarized level splitting
- In II, el-ph interaction U dominates, main polarization direction is along valley axis

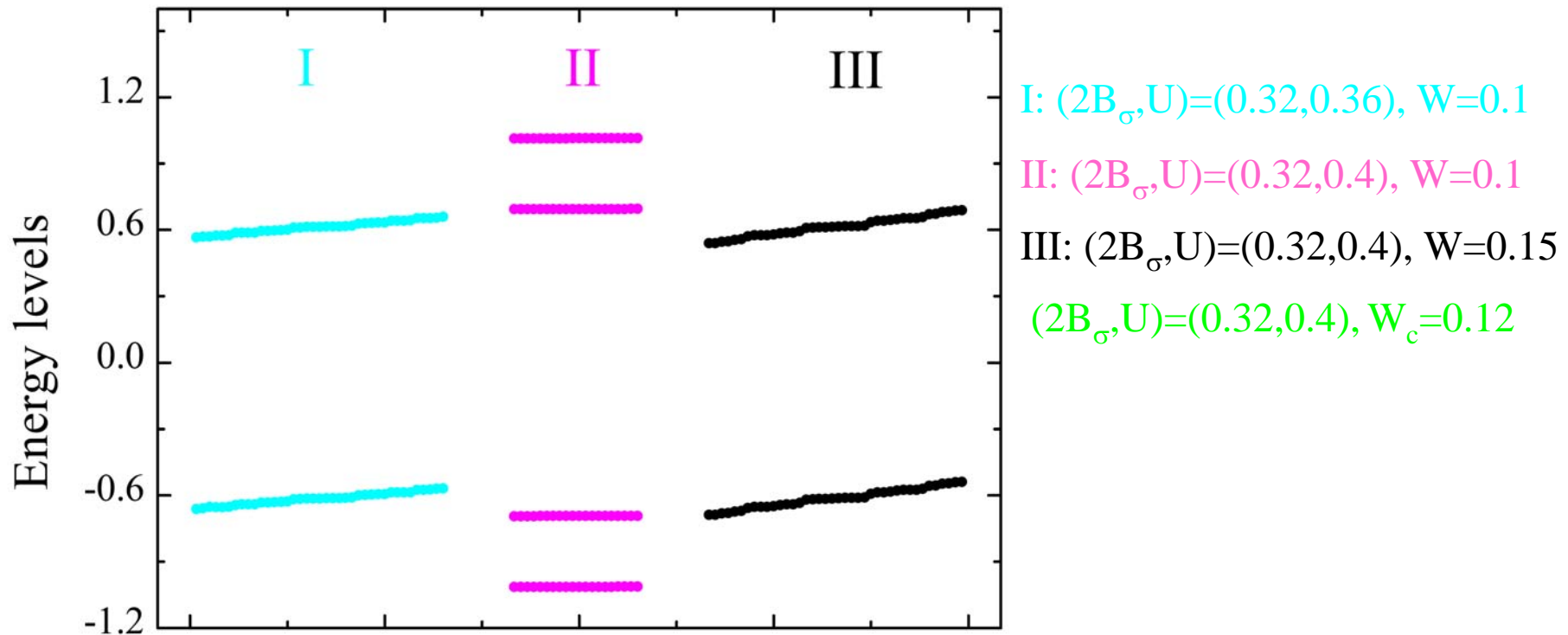
SCHFT: $H^{\text{EX}} + H^{\text{el-ph}} + H^{\text{B}}$ (quarter-filling case)



“valley-first” –split region I \longleftrightarrow “spin first” –split region II

SCHFT: $H^{\text{EX}} + H^{\text{el-ph}} + H^{\text{B}} + H^{\text{imp}}$ (half-filling case)

- Schematic energy levels



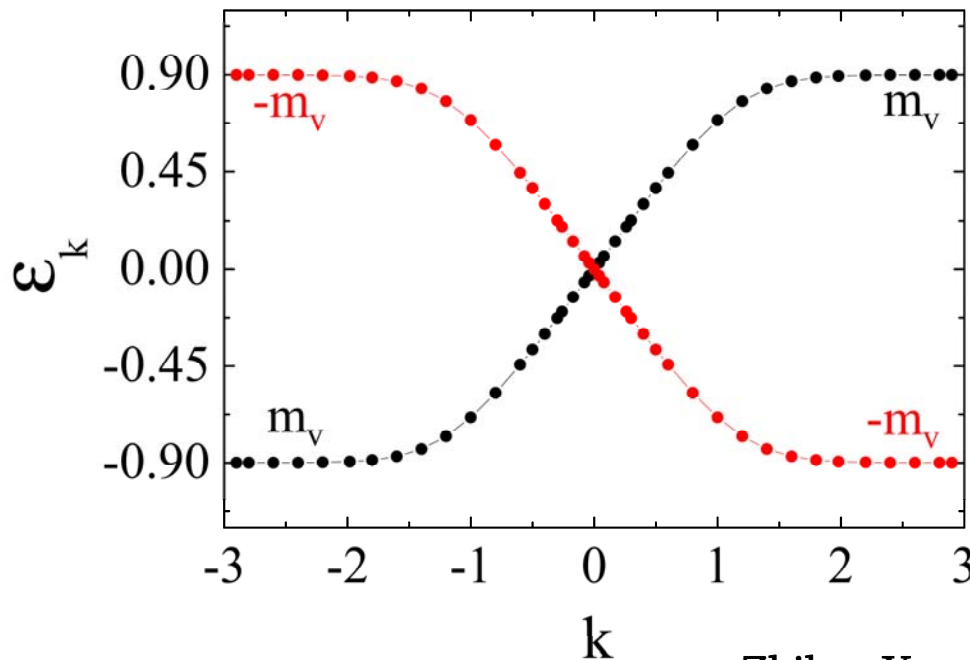
- In region I, the impurity does not alter the basic features of phase diagram $(2B_{\sigma}, U)$,
- In region II, the impurity does not alter the features of phase diagram $(2B_{\sigma}, U)$ when $W < W_c$,
- When $W > W_c$ the original 4-fold splitting levels in region II disappear \Rightarrow Region III.

Midgap states between LL of opposite valley polarities

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- Valley domain walls may exist because $E(\sigma,\tau)=E(\sigma,-\tau)$ due to Zeeman splitting
- Considering a spinless case first,

$$\begin{aligned} -i(y_k + \partial_y)v_+ + m(y)v_- &= \varepsilon_k u_+ \\ -i(y_k - \partial_y)v_- + m(y)v_+ &= \varepsilon_k u_- \\ i(y_k + \partial_y)u_- + m(y)u_+ &= \varepsilon_k v_+ \\ i(y_k - \partial_y)u_+ + m(y)u_- &= \varepsilon_k v_- \end{aligned}$$



Mass gap : $m(y) = m_v(y > 0)$
 $= -m_v(y < 0)$

Conclusion and Outlook

- Several microscopic mechanisms are explored=>breaking $n=0$ 4-fold LL degeneracy in a single-layer graphene
 - **Coulomb exchange, Zeeman interaction, valley-scattering impurity, electron-phonon interaction**
- The competitive nature of the valley-splitting(el-ph interaction) and spin-splitting(Zeeman interaction) leads to a phase diagram
 - **Either “spin first” or “valley first” level splitting**
- Gapless states exist when LLs with opposite valley polarities form a domain wall
- Our calculation suggests full LL splitting implies CDW order
- Graphene QHE in single and bilayers shows interesting symmetry breaking pattern
 - **Bilayer case will be more complicated**